Answers:
(1) Given that $\tan x=-\frac{24}{7}$


$$
\begin{aligned}
& h=\sqrt{24^{2}+(-7)^{2}}=25 \\
& \sin x=\frac{24}{25} \\
& \cos x=-\frac{7}{25} \\
& \sin x+2 \cos x=\frac{24}{25}+2\left(-\frac{7}{25}\right) \\
& \quad=\frac{10}{25}=\frac{2}{5}
\end{aligned}
$$

(2) (a) $\frac{\sin \angle A D B}{20}=\frac{\sin 28^{\circ}}{10}$

$$
\begin{aligned}
\sin \angle A D B & =2 \sin 28^{\circ} \\
\angle A D B & =69.9^{\circ} \text { or } 110.1^{\circ}
\end{aligned}
$$

Since $\angle A D B$ is obtuse, therefore $\angle A D B=110.1^{\circ}$
(b) $\angle B A C=180^{\circ}-28^{\circ}-110.1^{\circ}=41.9^{\circ}$

$$
\begin{aligned}
& \frac{B C}{20}=\sin 41.9^{\circ} \\
& B C=13.4 \mathrm{~cm}
\end{aligned}
$$

